Subject: Geometry

Grade: 9-12

Lesson Name: Inscribed Angles

CC Standards: CCSS.MATH.CONTENT.HSG.CA 1

NCTM Standards: Geometry - Analyze characteristics and properties of geometric shapes and develop mathematical arguments about geometric relationships.

Engage: The students will work in groups on a review test which covers the previous material.

Questions: 1) Where can we start? Are all of the sides congruent? What do the verticies do to the circle?

2) Can we construct a known triangle? What kind of triangle? What are the properties of the triangle? How have we divided the circle?

Explore: Using GeoGebra, students should discover the relationship between the measure of the central angle and an inscribed angle.

Questions: What is the measure of the angle we created? Does the angle change if we move the vertex?

Explain: The students will propose a valid definition of an inscribed angle.

Definition: An **inscribed angle** is an **angle** formed by two chords in a circle which have a common endpoint. This common endpoint forms the vertex of the **inscribed angle**. The other two endpoints **define** what we call an intercepted arc on the circle.

Questions: does any other figure fit our definition? Is there an alternate definition we could use? What are the segments called when dealing with a circle?

The students will use their explorations to propose a relationship between the angles.

The students will work as a class to prove the first case of an inscribed angle, as small groups to prove their proposal for the second case and share their results.

Questions: What is out hypothesis? What do we want to show?

Elaborate: The students will start with a loose definition of an inscribed angle and refine it until it is precise. Further the students will be asked for an alternate definition.

Using their GeoGebra, students will make a conjecture as to what happens to the measure of the angle if the vertex is moved between the intersection points.

Evaluate: The students previous knowledge will be evaluated with the pretest.

Their understanding of the topic will be evaluated via an 'Exit Ticket' by completing the $3^{\rm rd}$ case of the proof.

Questions: How is the 3^{rd} case similar to the 1^{st} and 2^{nd} ? How is it different? How can we make it similar to something we have proven?

Materials:

Pretest – printed and handed out at beginning of class

GeoGebra file 'Inscribed_Angle_Activity.ggb' – to be emailed during pretest

Exit Ticket – printed and handed out at end of lesson